

## TABLES

Table 1. List of initial simulation parameters and relevant non-dimensional numbers.

Case	A	B	C	D	E
$u'/S_L$	5.0	6.25	7.5	9.0	11.25
$l/\delta_{th}$	1.67	1.44	2.5	4.31	3.75
$Re_t$	22.0	23.5	49.0	100	110
$Da$	0.33	0.23	0.33	0.48	0.33
$Ka$	8.65	13.0	13.0	13.0	19.5

## FIGURE CAPTIONS

Figure 1: Distributions of reaction progress variable  $c$ , non-dimensional temperature  $T$  and non-dimensional reaction rate  $\dot{\omega} \times \delta_Z / \rho_0 S_L$  for turbulent case D with  $Le = 0.8, 1.0$  and  $1.2$  at  $t = \delta_Z / S_L, 2 \delta_Z / S_L, 4 \delta_Z / S_L, 6 \delta_Z / S_L, 8 \delta_Z / S_L$  on central  $x_1 - x_3$  plane.

Figure 2: Variations of  $\tilde{c}(1 - \tilde{c})$  (solid line) and  $\tilde{c}''^2$  (dash line) with  $x_1 / \delta_Z$  at different time instants for cases A-E (1<sup>st</sup>-5<sup>th</sup> columns) and  $Le = 0.8, 1.0$  and  $1.2$ .

Figure 3: Variations of  $T_{1c}$ , —;  $T_{2c}$ , —;  $T_{3c}$ , —;  $D_{1c}$ , —;  $(-D_{2c})$ , — with  $x_1 / \delta_Z$  at  $t = 4\delta_Z / S_L, 6\delta_Z / S_L, 8\delta_Z / S_L, 10\delta_Z / S_L$  for turbulent cases A-E with  $Le = 0.8, 1.0$  and  $1.2$ .

Figure 4: Variations of  $\overline{\rho u_1'' c''^2}$  extracted from DNS data (solid line) along with the predictions of Eqs. 9 (dotted line) and 10 (broken line) with  $x_1 / \delta_Z$  at  $t = 4\delta_Z / S_L, 6\delta_Z / S_L, 8\delta_Z / S_L, 10\delta_Z / S_L$  for turbulent cases A-E with  $Le = 0.8, 1.0$  and  $1.2$ . Please refer to the table in Fig. 2 for the colour scheme.

Figure 5: Variations of  $\overline{\rho u_1'' c''}$  extracted from DNS data (solid line) along with the predictions of Eqs. 14 (dotted circle line) and 15 (broken triangle line) with  $x_1 / \delta_Z$  at  $t = 4\delta_Z / S_L, 6\delta_Z / S_L, 8\delta_Z / S_L, 10\delta_Z / S_L$  for turbulent cases A-E with  $Le = 0.8, 1.0$  and  $1.2$ . Please refer to the table in Fig. 2 for the colour scheme.

Figure 6: Variations of  $T_{3c}$  extracted from DNS data (solid line) along with the predictions of Eqs. 18 (dotted circle line) and 20 (broken triangle line) with  $x_1 / \delta_Z$  at

$t = 4\delta_Z/S_L$  ,  $6\delta_Z/S_L$  ,  $8\delta_Z/S_L$  ,  $10\delta_Z/S_L$  for turbulent cases A-E with  $Le = 0.8$ , 1.0 and 1.2. Please refer to the table in Fig. 2 for the colour scheme.

Figure 7: Variations of  $\bar{\omega}^+ = \bar{\omega} \times \delta_Z/\rho_0 S_L$  with  $x_1/\delta_Z$  along with the predictions of Eq. 19a at  $t = 4\delta_Z/S_L$  ,  $6\delta_Z/S_L$ ,  $8\delta_Z/S_L$ ,  $10\delta_Z/S_L$  for turbulent cases A-E with  $Le = 0.8$ , 1.0 and 1.2.

Figure 8: Variations of  $\bar{\varepsilon}_c^+ = \bar{\varepsilon}_c \times \delta_Z/S_L$  obtained from DNS data and the predictions of Eqs. 21 and 24 with  $x_1/\delta_Z$  at  $t = 4\delta_Z/S_L$  ,  $6\delta_Z/S_L$  ,  $8\delta_Z/S_L$  ,  $10\delta_Z/S_L$  for turbulent cases A-E with  $Le = 0.8$ , 1.0 and 1.2. Please refer to the table in Fig. 2 for the colour scheme.

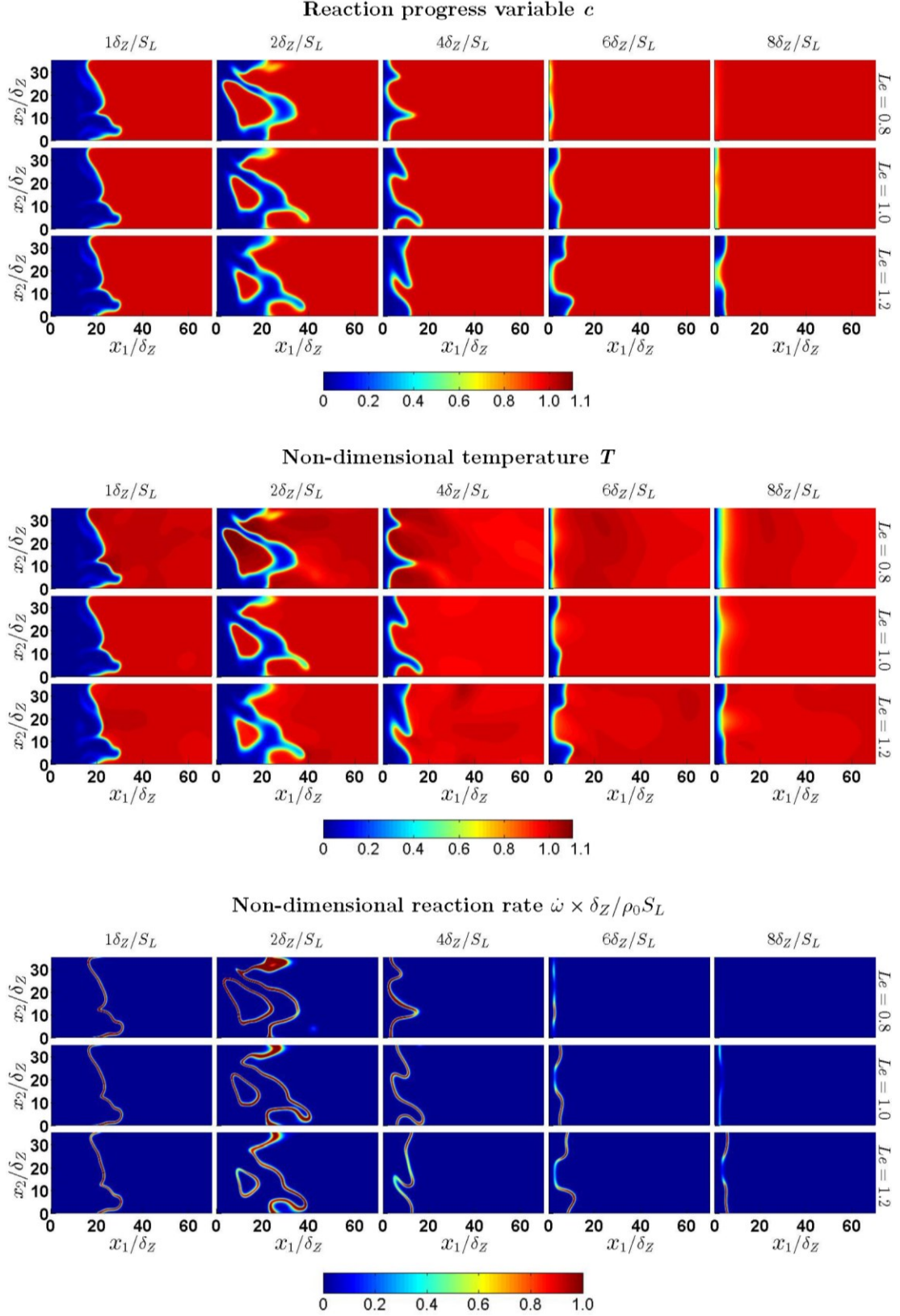


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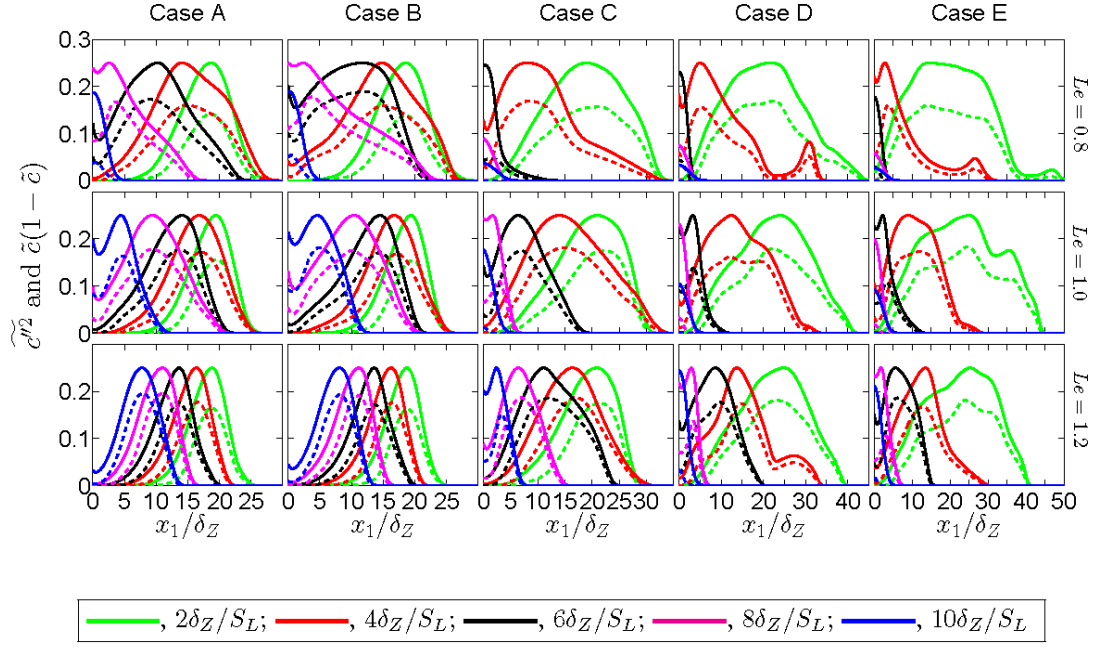


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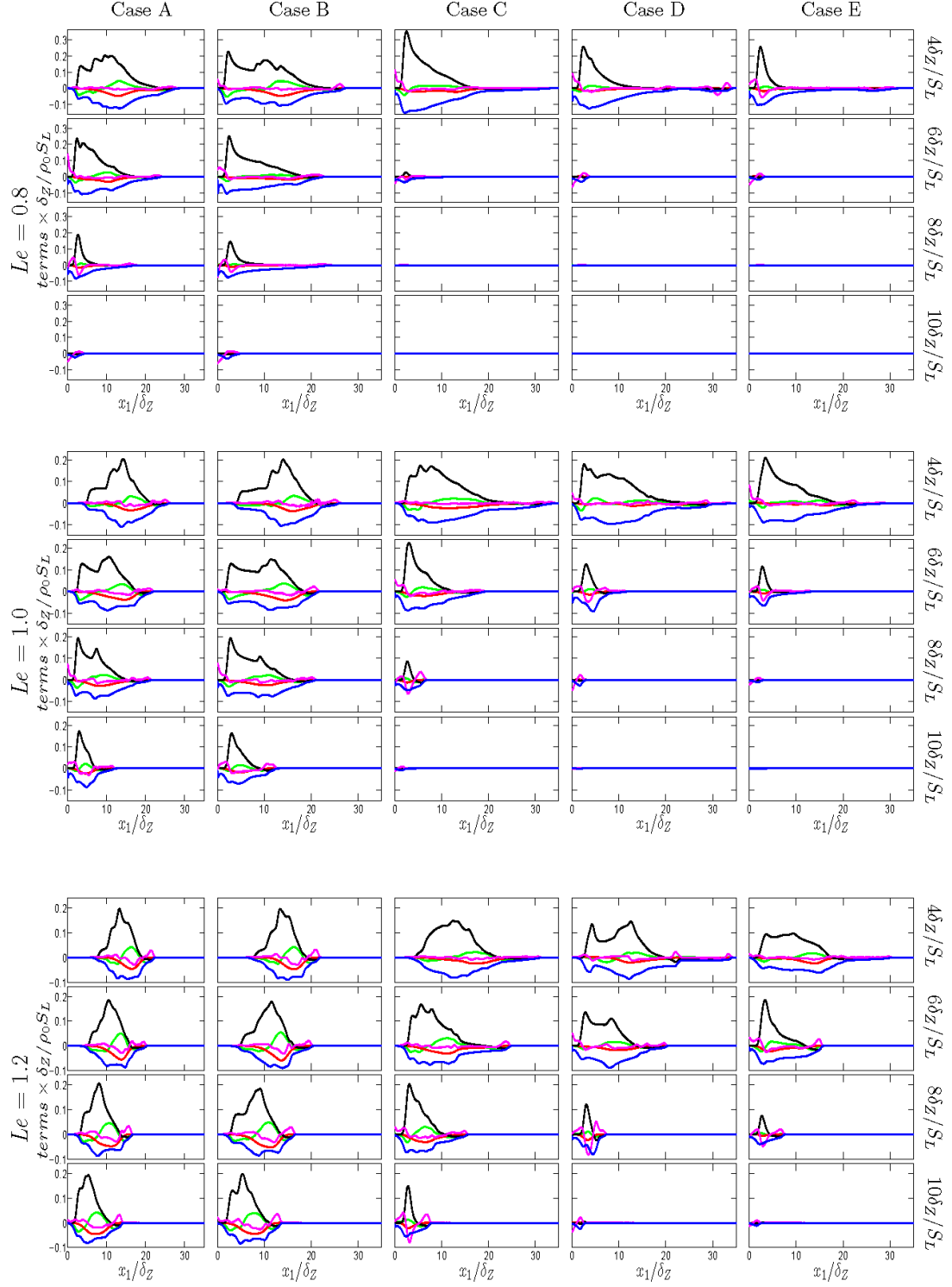


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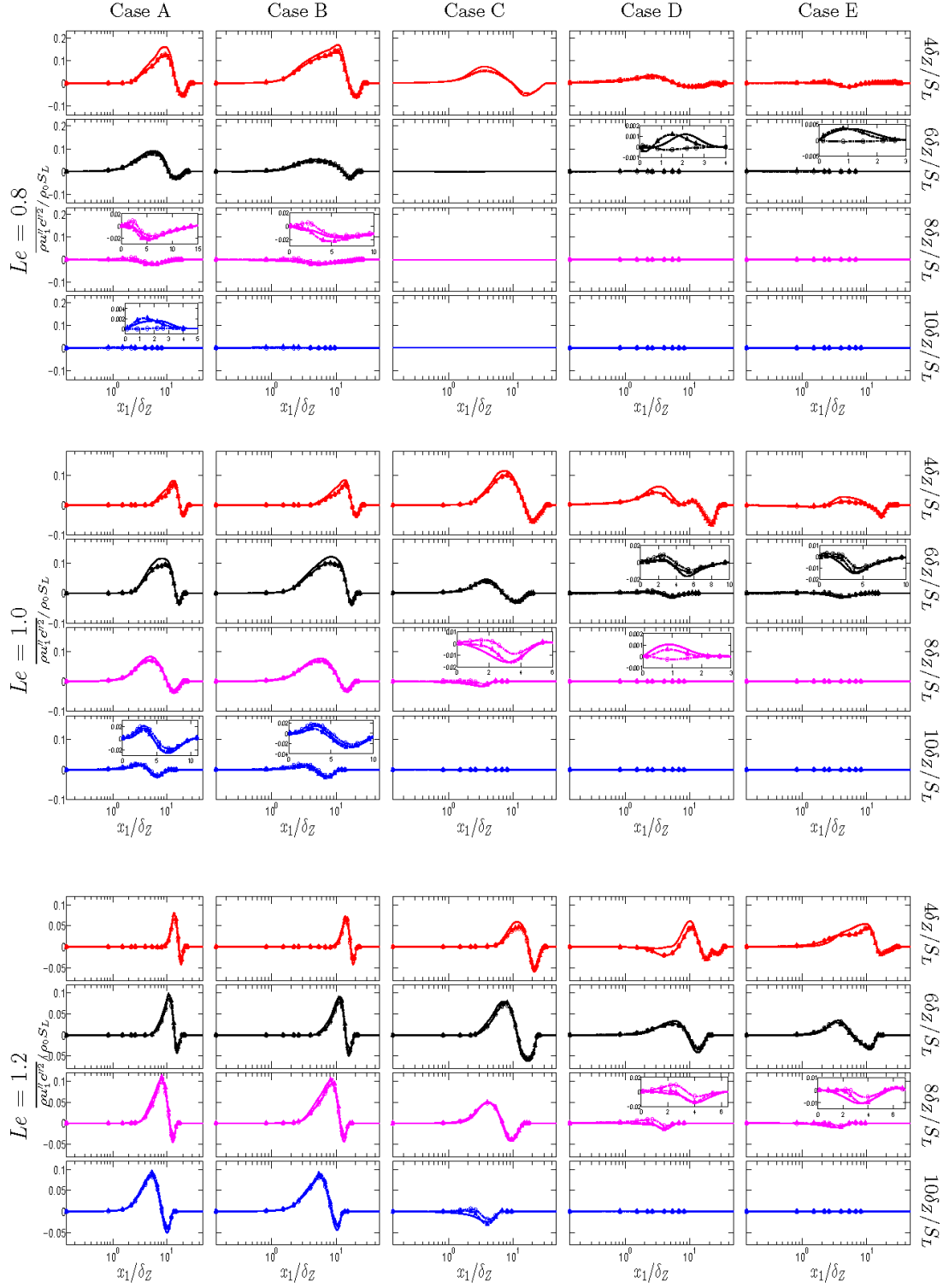


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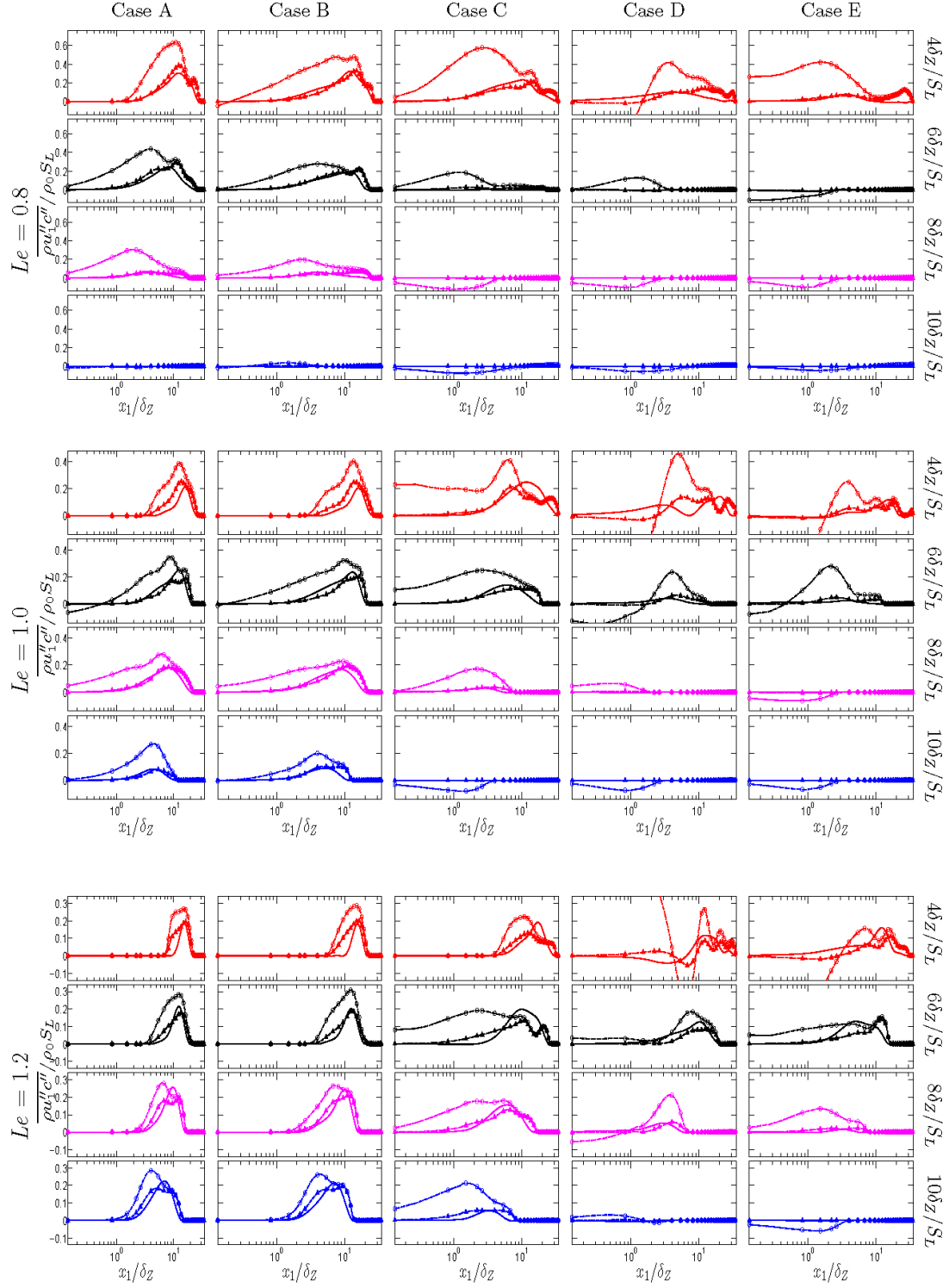


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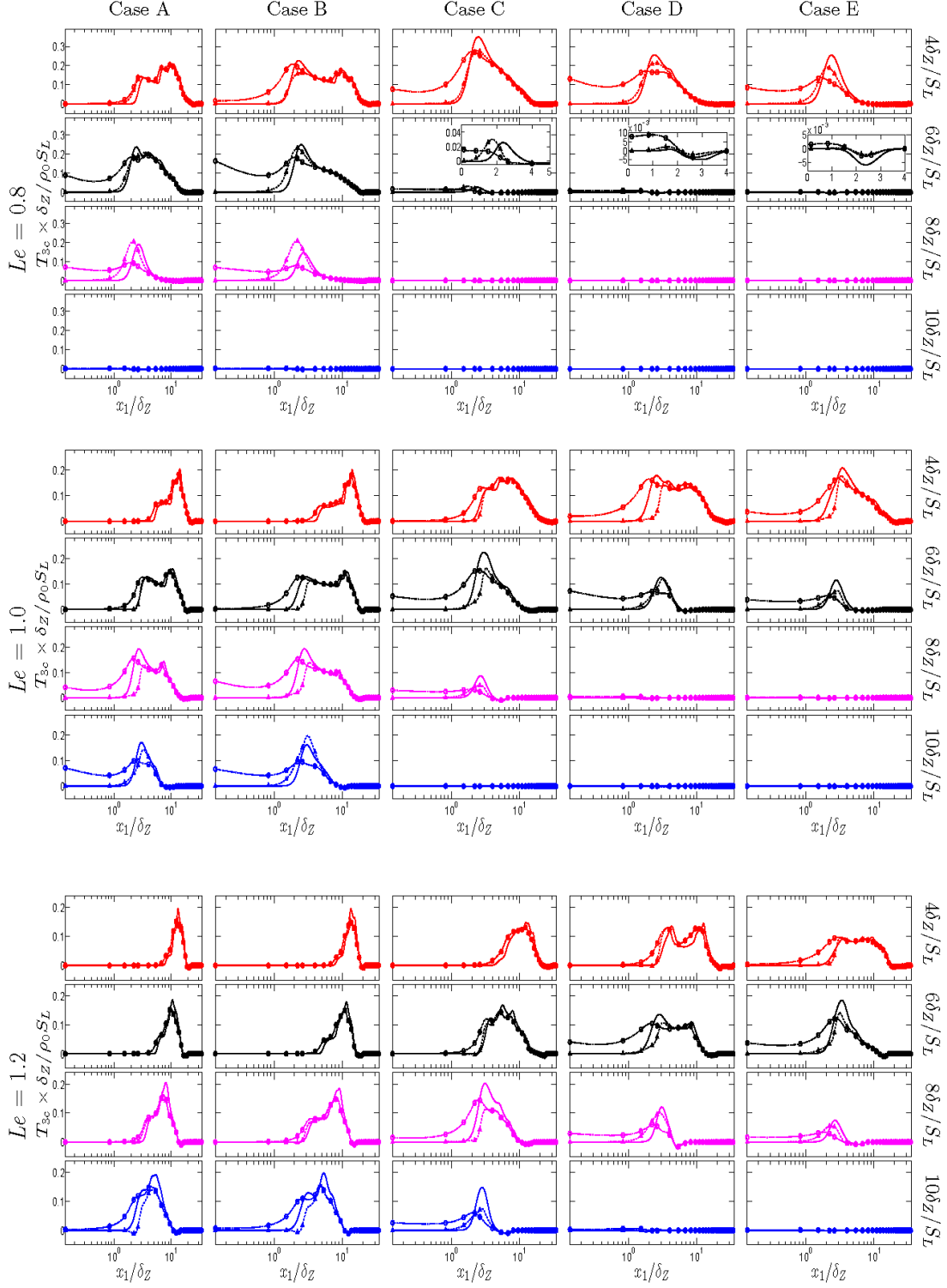
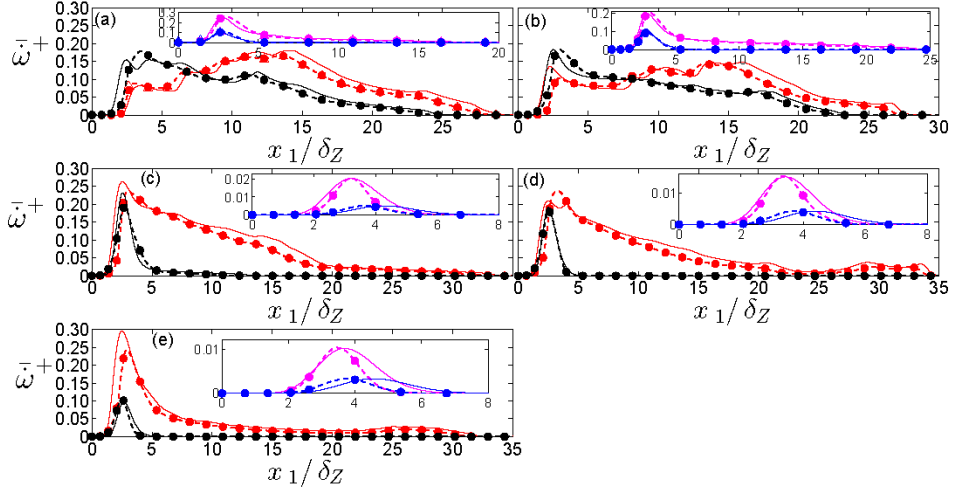
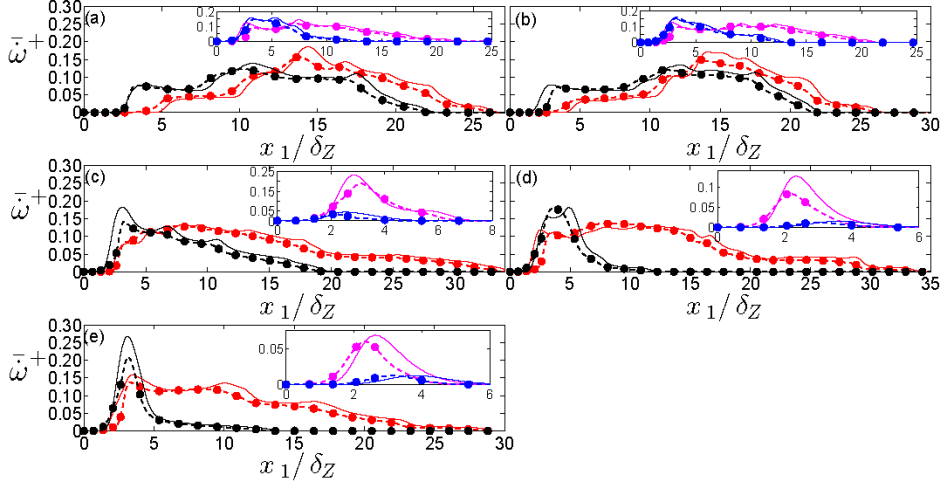


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$Le = 0.8$



$Le = 1.0$



$Le = 1.2$

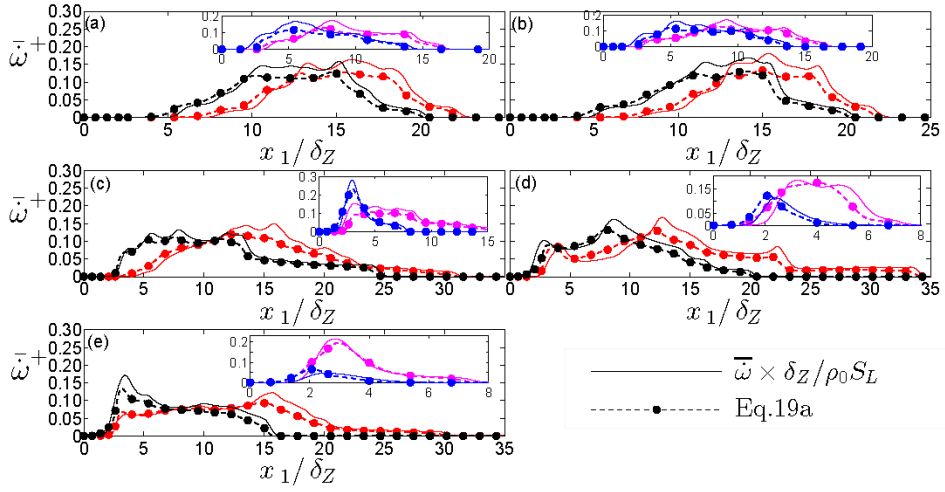
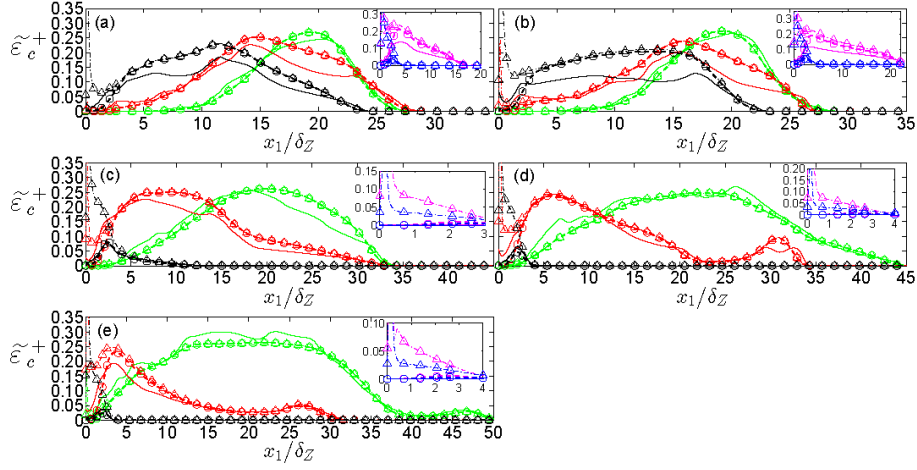
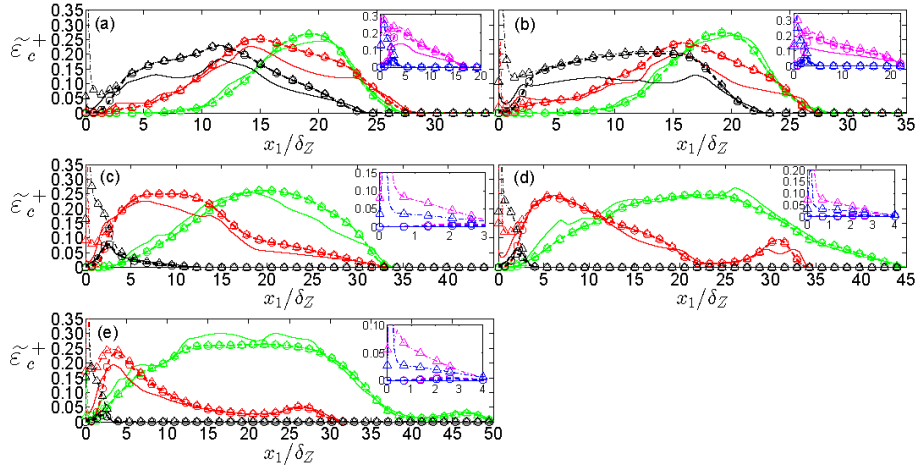


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$Le = 1.0$



$Le = 1.2$

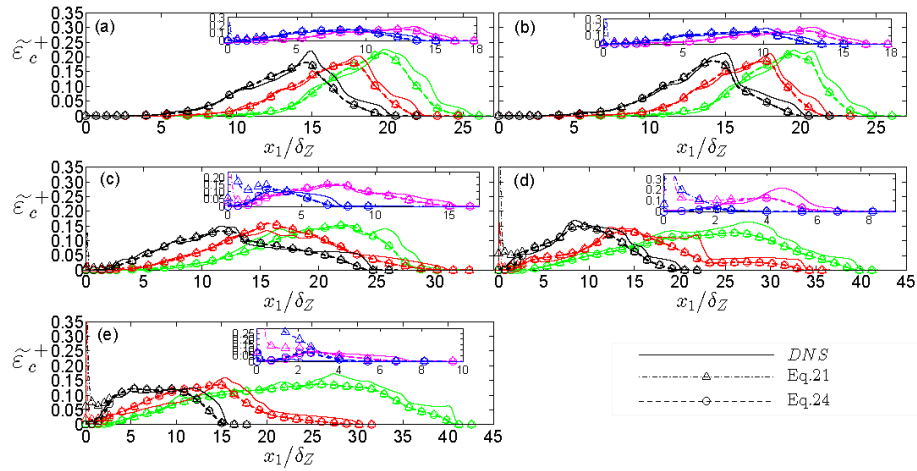


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