

# Engineering Dark Solitary waves in Ring-Trap Bose-Einstein condensates

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## 1. Captions to movies

Fixed parameters throughout the movies.

*Ring-trap:*

- $\omega_{\perp} = 2\pi 600$  Hz
- $V_G = 31.5 k_B$  nK
- $\mathbf{r}_0 = 1.85 l_0$
- $\omega = 0.95 l_0$

Reference length unit:  $l_0 = 10 \mu\text{m}$ .

Density is given in units of  $l_0^{-2}$ .

*Perturbation:*

- $V_0/\mu = 2$
- $\sigma/\xi = 0.7$

## MOVIES

**1d.solitonic.avi:** Renormalized density (top) and phase (bottom) profiles showing the mean-field evolution of density engineered counterpropagating solitary waves in a ring-trap (see Fig. A3 in the manuscript) in the 1d solitonic regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 1.1$  nm
- $l_r/\xi = 0.8$
- $N = 12200$
- $T = 0$

**2d.solitonic.avi:** Renormalized density (top) and phase (bottom) profiles showing the mean-field evolution of density engineered counterpropagating solitary waves in a ring-trap (see Fig. 4a in the manuscript) in the 2d solitonic regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 2.75\text{nm}$
- $l_r/\xi = 1.3$
- $N = 15600$
- $T = 0$

**shedding.avi:** Renormalized density (top) and phase (bottom) profiles showing the mean-field evolution of density engineered counterpropagating solitary waves in a ring-trap (see Fig. 4b in the manuscript) in the shedding regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 4.07\text{nm}$
- $l_r/\xi = 1.54$
- $N = 18600$
- $T = 0$

**snaking.avi:** Renormalized density (top) and phase (bottom) profiles showing the mean-field evolution of density engineered counterpropagating solitary waves in a ring-trap (see Fig. 4c in the manuscript) in the snaking regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 8.25\text{nm}$
- $l_r/\xi = 2.2$
- $N = 28200$
- $T = 0$

**2d.solitonic.long.evolution.avi:** Renormalized density (top) and phase (bottom) profiles showing the long-term mean-field evolution of density engineered counterpropagating solitary waves in a ring-trap (see Fig. 4a in the manuscript) in the 2d solitonic regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 2.75\text{nm}$
- $l_r/\xi = 1.3$
- $N = 15600$
- $T = 0$

**2d.solitonic.T9nK.avi:** Renormalized density (top) and phase (bottom) profiles showing the long-term stochastic dynamics of density engineered counterpropagating solitary waves in a ring-trap (see Fig. 6 in the manuscript) in the 2d solitonic regime (see Fig. 3 in the manuscript). Gas parameters:

- $a_s = 2.75\text{nm}$
- $l_r/\xi = 1.3$
- $N = 18700$
- $T = 9\text{nK}$